

## Ordinary Differential Equations - Part 21



 $= \left( \alpha + \gamma_{t_0, X_0} \right)^{\bullet} (t)$  $\implies \alpha + \gamma_{t_0, X_0} \in S$ 

Then: 
$$\alpha + \gamma_{t_0, \chi_0} \in S$$
 with  $(\alpha + \gamma_{t_0, \chi_0})(t_0) = \alpha(t_0) + \gamma_{t_0, \chi_0}(t_0)$   
 $= \tilde{\chi}_0 - \chi_0 + \chi_0 = \tilde{\chi}_0$   
 $\implies \alpha + \gamma_{t_0, \chi_0}$  is solution of  $(IVP_{\chi_0}^{t_0})$   
Aniqueness  
 $\implies \beta = \alpha + \gamma_{t_0, \chi_0}$ 

Result: The solution set of  $\dot{x} = A(t)x + b(t)$  is given by

$$S = S_{\circ} + \gamma$$

where  $S_{o}$  is the solution space of the homogeneous part  $\dot{x} = A(t) x$ and  $\gamma$  is a particular solution of  $\dot{x} = A(t) x + b(t)$ .  $\left(S$  is an n-dimensional affine subspace  $\right)$