ON STEADY

Nn



Manifolds - Part 37

 $M \subseteq \mathbb{R}^3$ orientable Riemannian manifold of dimension 2

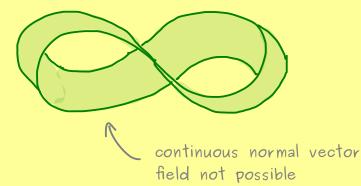
- length of N $\leftrightarrow \rightarrow$ canonical volume form

We call it a continuous unit normal vector field if

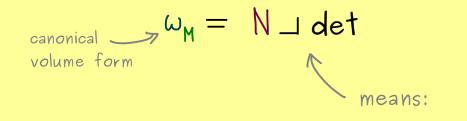
• N is continuous at every $p \in M$ • $\|N(x)\| = \sqrt{g_x(N(x), N(x))} = 1$ for all $x \in M$.

<u>Important fact</u>: $M \subseteq \mathbb{R}^n$ (n-1)-dimensional submanifold:

(a) M is orientable $\iff M$ has a continuous unit normal vector field

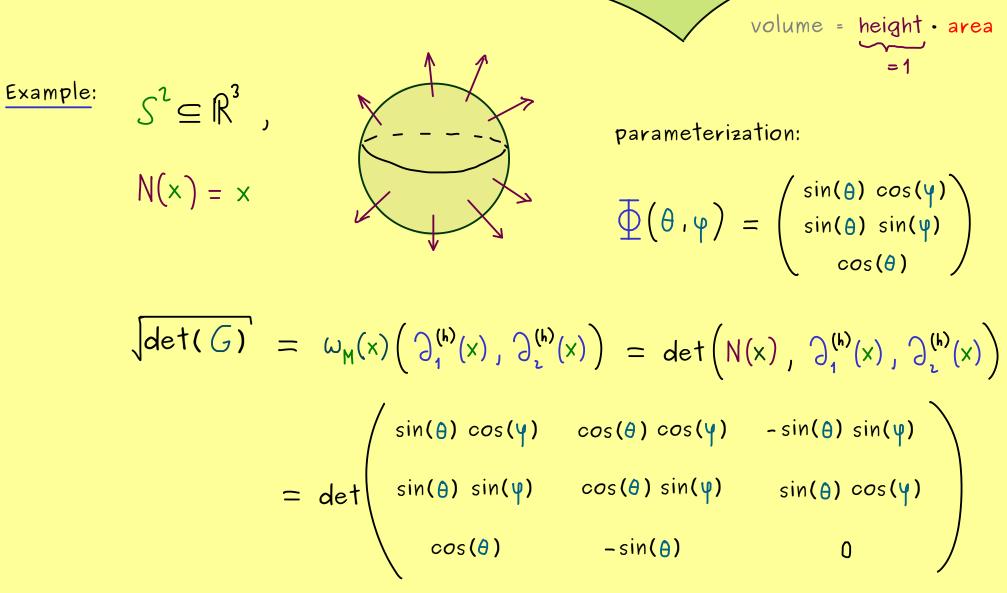


(b) If N is a continuous unit normal vector field, then:



 $\omega_{\mathsf{M}}(\mathsf{x})(\mathsf{V}_{1},\ldots,\mathsf{V}_{\mathsf{n-1}}) = \mathsf{det}(\mathsf{N}(\mathsf{x}),\mathsf{V}_{1},\ldots,\mathsf{V}_{\mathsf{n-1}})$





 $= sin(\theta)$