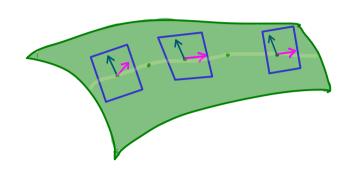


Manifolds - Part 32

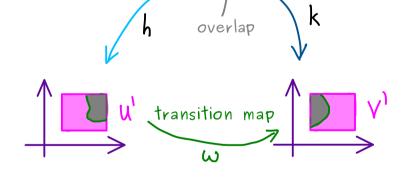


orientable manifold M

Fact: Let M be an n-dim smooth manifold. Then the following claims are equivalent:

- (a) M is <u>orientable</u>: We have $\left\{ \left(T_{p}M, or_{p} \right) \right\}$ such that $\forall p \in M \ \exists \left(U, h \right) \ \forall x \in U : \left(\partial_{1}^{(h)}(x), \partial_{2}^{(h)}(x), \dots, \partial_{n}^{(h)}(x) \right) \in or_{x}$

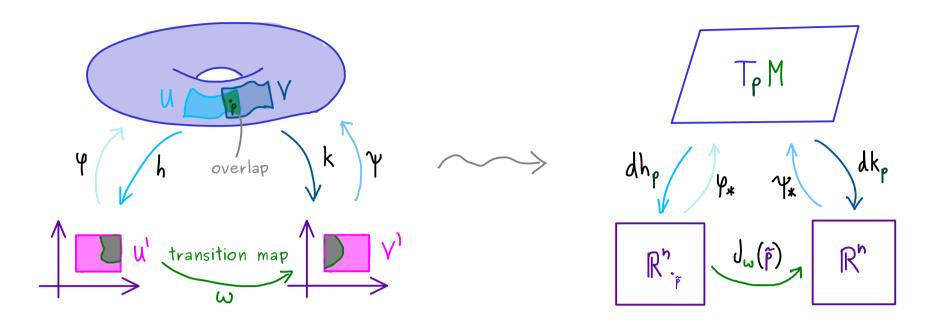
$$det(J_{\omega}(x)) > 0$$



(c) There is a differential form (volume form)

$$\omega \in \Omega^{n}(M)$$
 with $\omega(p) \neq 0$ for all $p \in M$.

Proof: (a) \iff (b)



Hence:

$$\det(\mathsf{T}_{c\in\mathcal{B}})>0\iff\det(\mathsf{J}_{\omega}(\mathsf{x}))>0$$
(a) \iff (b)