

Manifolds - Part 22

smooth manifold M of dimension n , $p \in M$.

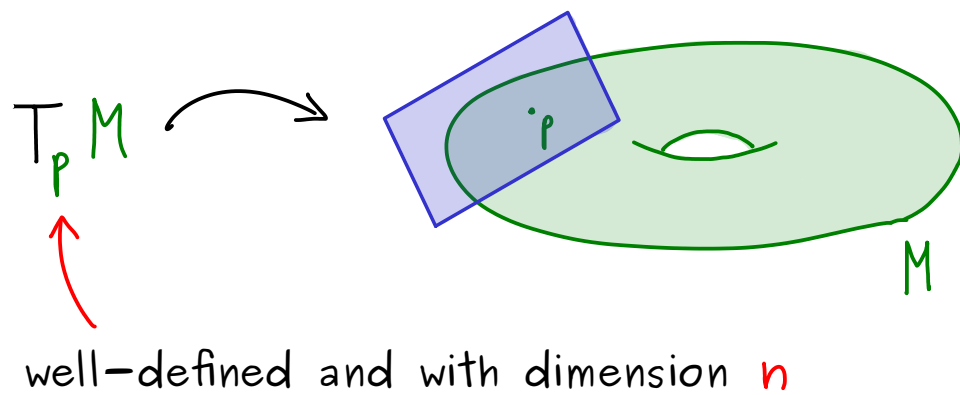
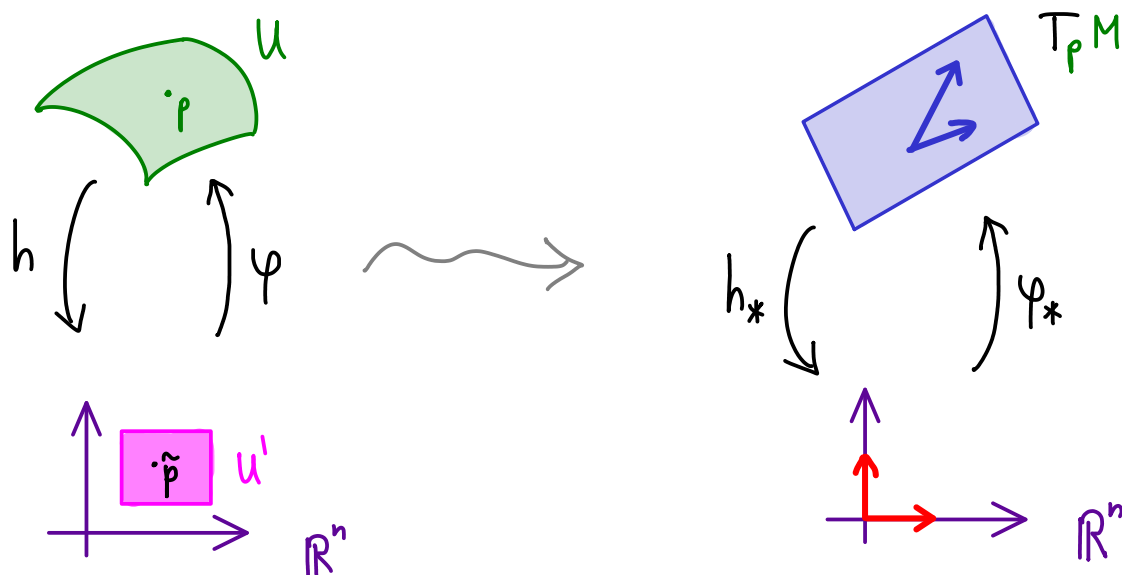


chart (U, h) :



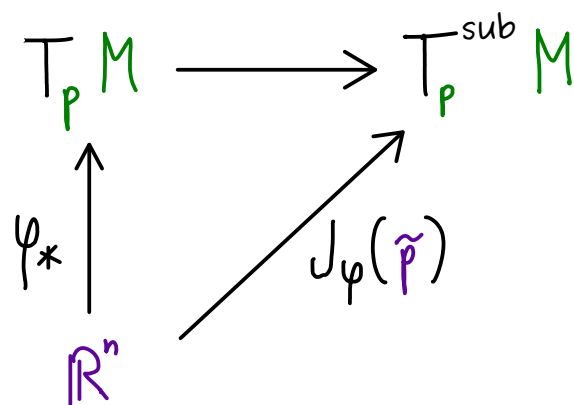
defined by:
 $h_* : T_p M \rightarrow \mathbb{R}^n$
 $[\gamma] \mapsto (h \circ \gamma)'(0)$
 linear + bijective
 $\psi_* := h_*^{-1}$

Definition: coordinate basis (standard basis with respect to (U, h)):

For (U, h) and $p \in U$, we define: $\partial_j := \psi_*(e_j)$

where (e_1, e_2, \dots, e_n) is the standard basis of \mathbb{R}^n

Remember: For submanifolds:



$(\partial_1, \partial_2, \dots, \partial_n)$ is essentially $\left(\frac{\partial \psi}{\partial x_1}(\tilde{p}), \frac{\partial \psi}{\partial x_2}(\tilde{p}), \dots, \frac{\partial \psi}{\partial x_n}(\tilde{p}) \right)$

Soon: $f: M \rightarrow N$ smooth \rightsquigarrow $df_p: T_p M \rightarrow T_p N$ differential