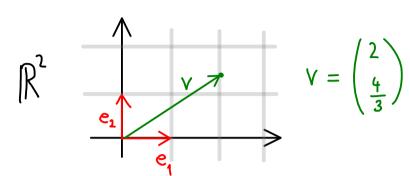
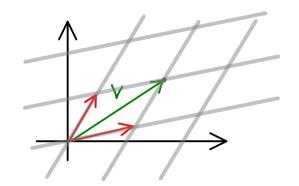


## Linear Algebra - Part 25

basis of a subspace: spans the subspace + linearly independent



$$V = \begin{pmatrix} 2 \\ \frac{4}{3} \end{pmatrix}$$



coordinates

coordinates:

$$U \subseteq \mathbb{R}^n$$

 $\mathcal{U} \subseteq \mathbb{R}^{h}$  subspace,  $\mathcal{B} = (\mathbf{V}^{(1)}, \mathbf{V}^{(1)}, \dots, \mathbf{V}^{(k)})$  basis of  $\mathcal{U}$ 

$$(V^{(k)})$$

 $\Longrightarrow$  Each vector  $u \in \mathcal{U}$  can be written as a linear combination:

$$U = \lambda_1 V^{(1)} + \lambda_2 V^{(2)} + \cdots + \lambda_k V^{(k)}$$

coordinates of u with respect to  ${\mathcal B}$ 

$$\mathbb{R}^{3} = \operatorname{Span}\left(\begin{pmatrix} -3 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 2 \\ 0 \\ -1 \end{pmatrix}\right)$$

 $U = \begin{pmatrix} 1 \\ 2 \end{pmatrix} = 1 \cdot \begin{pmatrix} -3 \\ 0 \end{pmatrix} + 2 \cdot \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} + 1 \cdot \begin{pmatrix} 2 \\ 0 \\ -1 \end{pmatrix}$ 

$$\widetilde{U} = \begin{pmatrix} 3 \\ 0 \\ 0 \end{pmatrix} = -1 \cdot \begin{pmatrix} -3 \\ 0 \\ 0 \end{pmatrix} + \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} + \begin{pmatrix} 2 \\ 0 \\ -1 \end{pmatrix}$$