

## Linear Algebra - Part 15

AERmxn collection of m row vectors

$$A = \begin{pmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{pmatrix} = \begin{pmatrix} -\alpha_1^T & ---- \\ -\alpha_2^T & ---- \\ ---- & ----- \\ ----- & ---- \\ ----- & ---- \\ ----- & ---- \\ ----- & ----- \\$$

$$\alpha_{i}^{T} := (\alpha_{i1} \ \alpha_{i2} \ \cdots \ \alpha_{in})$$

$$T \text{ stands for "transpose"}$$

flat matrix
$$\mathbb{R}^{1\times n} = \begin{pmatrix} \mathbf{u}_1 \\ \mathbf{u}_2 \\ \vdots \\ \mathbf{u}_n \end{pmatrix} = \begin{pmatrix} \mathbf{u}_1 & \mathbf{u}_2 & \cdots & \mathbf{u}_n \end{pmatrix}$$
transpose of column vector row vector

 $u^T X$  for  $X \in \mathbb{R}^n$  is defined.

standard inner produc

For  $u, y \in \mathbb{R}^n$ :  $u^T y = \langle u, y \rangle$ Remember:

Row picture of the matrix-vector multiplication:

$$A \times = \begin{pmatrix} - & \alpha_{1}^{\mathsf{T}} - & \\ & - & \alpha_{2}^{\mathsf{T}} - \\ & \vdots & \\ & - & \alpha_{m}^{\mathsf{T}} - \end{pmatrix} \begin{pmatrix} & & \\ &$$

$$\begin{pmatrix} 2 & 1 & 2 \\ 3 & 2 & 1 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 2 \cdot 3 + 1 \cdot 1 + 2 \cdot 0 \\ 3 \cdot 3 + 2 \cdot 1 + 1 \cdot 0 \end{pmatrix} = \begin{pmatrix} 7 \\ 11 \end{pmatrix}$$