ON STEADY

The Bright Side of Mathematics



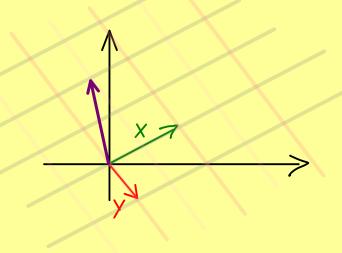
Linear Algebra - Part 64

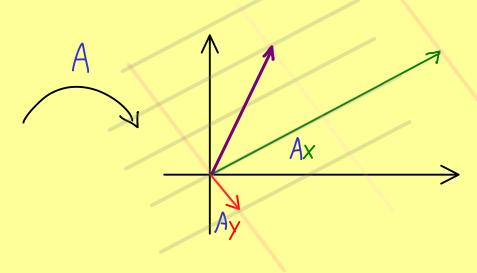
Diagonalization = transform matrix into a diagonal one find a an optimal coordinate system

Example:

$$A = \begin{pmatrix} 3 & 2 \\ 1 & 2 \end{pmatrix}, \quad \lambda_1 = 4, \quad \lambda_2 = 1 \quad \text{(eigenvalues)}$$

$$x = \begin{pmatrix} 2 \\ 1 \end{pmatrix}, \quad y = \begin{pmatrix} 1 \\ -1 \end{pmatrix} \quad \text{(eigenvectors)}$$





$$\propto \times + \beta \gamma \qquad \longmapsto \qquad \propto \lambda_1 \times + \beta \lambda_2 \gamma$$

 $A \in \mathbb{C}^{h \times n} \longrightarrow \lambda_1, \lambda_2, \dots, \lambda_n$ (counted with algebraic multiplicities) Diagonalization: \rightarrow $\chi^{(1)}, \chi^{(2)}, \dots, \chi^{(n)}$ (associated eigenvectors)

$$\rightarrow$$
 $A x^{(1)} = \lambda_1 x^{(1)}, \dots, A x^{(n)} = \lambda_n x^{(n)}$ (eigenvalue equations)

$$\Longrightarrow$$
 $AX = XD$

$$\supset = X^{-1}AX$$

If X is invertible, then: $\mathcal{J} = X^{-1}AX$ A is similar to a diagonal matrix

 $A^{38} = (X \mathcal{D} X^{-1})^{38} = X \mathcal{D} \underbrace{X^{-1} X}_{1} \mathcal{D} \underbrace{X^{-1} X}_{1} \mathcal{D} \underbrace{X^{-1} X}_{1} \mathcal{D} X^{-1} \cdots X \mathcal{D} X^{-1}$

$$= \times \mathfrak{I}^{38} \times^{-1}$$

$$= \times \begin{pmatrix} \lambda_{1}^{98} & \\ \lambda_{2}^{98} & \\ & \lambda_{n}^{98} \end{pmatrix} \times^{-1}$$