ON STEADY

## The Bright Side of Mathematics



## Linear Algebra - Part 39

Goal:

Gaussian elimination

(named after Carl Friedrich Gauß)

solve Ax = 6

backwards substitution:

third row: 
$$3 \times_3 = 1 \implies X_3 = \frac{1}{3}$$

second row:  $2 \times_2 + \times_3 = 1 \implies X_2 = \frac{1}{3}$ 

first row:  $1 \times_1 + 2 \times_2 + 3 \times_3 = 1 \implies X_1 = -\frac{2}{3}$ 

or use row operations to bring (A|b) into row echelon form

> construct solution set

Example: system of linear equations:

$$2 x_{1} + 3 x_{2} - 1 x_{3} = 4$$

$$2 x_{1} - 1 x_{2} + 7 x_{3} = 0$$

$$6 x_{1} + 13 x_{2} - 4 x_{3} = 9$$

set of solutions:  $S = \begin{cases} 3 \\ -1 \\ -1 \end{cases}$ 

Gaussian elimination: