ON STEADY

The Bright Side of Mathematics



Linear Algebra - Part 24





$$U \subseteq \mathbb{R}^n$$
 with

plane:
$$\mathbb{R}^2$$
 Span $(v^{(1)}, v^{(2)}, v^{(3)}, v^{(4)}) = \mathbb{R}^2$

$$V^{(3)} V^{(1)} V^{(1)}$$
 Span $(V^{(1)}, V^{(3)}) = \mathbb{R}^1$

Span(
$$v^{(1)}, v^{(4)}$$
) = $\mathbb{R} \times \{0\} \neq \mathbb{R}^2$

Definition: $U \subseteq \mathbb{R}^n$ subspace, $\mathcal{B} = (V^{(1)}, V^{(1)}, \dots, V^{(k)})$, $V^{(j)} \in \mathbb{R}^n$.

 \mathfrak{F} is called a basis of \mathfrak{h} if:

(a)
$$U = Span(B)$$

(b) B is linearly independent

Example:

$$\mathbb{R}^n = \operatorname{Span}(e_1, \dots, e_n)$$

standard basis of Rh

$$\mathbb{R}^{3} = \operatorname{Span}\left(\begin{pmatrix} -3 \\ 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}, \begin{pmatrix} 2 \\ 0 \\ -1 \end{pmatrix}\right)$$
basis of \mathbb{R}^{3}