



step functions: consider the complex vector space:

 $\int_{2\pi - per} (\mathbb{R}, \mathbb{C}) := \begin{cases} g \in \mathcal{F}_{2\pi - per}(\mathbb{R}, \mathbb{C}) \mid \text{there are } m \in \mathbb{N}, a_i \in [-\pi, \pi], \\ \lambda_i \in \mathbb{C} \text{ such that}: \\ g = \sum_{i=1}^{m} \lambda_i \cdot h_{a_i} \end{cases}$ adding



Do we have Parseval's identity here?



$$C_{k} = \langle e_{k}, g \rangle = \langle e_{k}, \sum_{i=1}^{m} \lambda_{i} \cdot h_{a_{i}} \rangle = \sum_{i=1}^{m} \lambda_{i} \langle e_{k}, h_{a_{i}} \rangle$$

<u>Result:</u> Parseval's identity holds for $\int_{2\pi - per} (\mathbb{R}, \mathbb{C}) \subseteq \int_{2\pi - per}^{2} (\mathbb{R}, \mathbb{C})$.