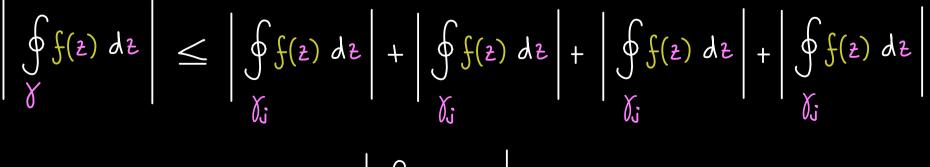
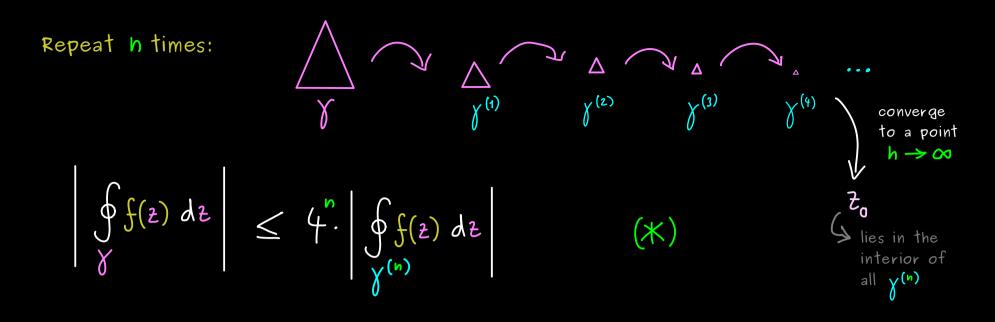
Complex Analysis - Part 22

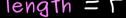
Goursat's theorem: $\int : \mathbb{D} \longrightarrow \mathbb{C}$ holomorphic, $\gamma: [a, b] \longrightarrow \bigcirc$ closed curve where the image is a triangle and the inner part lies in \mathbb{D} . not allowed $\oint f(z) dz = 0$ Then: Basic idea: $0 = \int_{\mathcal{T}} + \int_{\mathcal{F}} = \oint_{\mathcal{T}} + \int_{\mathcal{F}} = \oint_{\mathcal{T}} + \int_{\mathcal{F}} = \oint_{\mathcal{T}} + \int_{\mathcal{F}} + \int_{\mathcal{F}} = \int_{\mathcal{F}} + \int_{\mathcal{F}} = \int_{\mathcal{F}} + \int_{\mathcal{F}} + \int_{\mathcal{F}} = \int_{\mathcal{F}} + \int_{\mathcal$ Proof: Decompose triangle: $\int_{1}^{1} + \int_{2}^{2} + \int_{3}^{2} + \int_{4}^{4}$ $\oint f(z) dz = \oint f(z) dz$ ×1 + ×2 + ×3 + ×4 $= \oint f(z) dz + \oint f(z) dz + \oint f(z) dz + \oint f(z) dz$ Y1 82)] 84





differentiability at Z: Complex

$$\begin{vmatrix} \oint_{\gamma(*)} f(z) dz \\ = \begin{vmatrix} \oint_{\gamma(*)} \varphi(z) dz \\ \vdots \\ \gamma(*) \end{vmatrix} \leq \max_{z \in \operatorname{Ran}(\gamma^{(*)})} |\varphi(z)| \cdot \operatorname{Iength}(\gamma^{(*)}) \\ \leq \max_{z \in \operatorname{Ran}(\gamma^{(*)})} |\varphi(z)| \cdot \max_{z \in \operatorname{Ran}(\gamma^{(*)})} |z - z_{o}| \cdot \operatorname{Iength}(\gamma^{(*)}) \\ = \frac{\Gamma}{2^{10}} \frac{\Gamma}{2^{10}} \\ \vdots \\ \gamma^{(1)} |\operatorname{Iength} \frac{\Gamma}{2} \\ \gamma^{(1)} |\operatorname{Iength} \frac{\Gamma}{2} \\ \gamma^{(1)} |\operatorname{Iength} \frac{\Gamma}{2^{10}} \\ \vdots \\ \gamma^{(1)} |\operatorname{Iengt} \frac{\Gamma}{2^{10}} \\ \vdots \\$$



 $\left| \oint_{\chi} f(z) dz \right| \stackrel{(*)}{\leq} 4^{n} \cdot \left| \oint_{\chi(n)} f(z) dz \right| \leq \Gamma^{2} \cdot \max_{z \in \operatorname{Ran}(\chi(n))} |\psi(z)| \stackrel{h \to \infty}{\longrightarrow} 0$