



## Complex Analysis - Part 1

analysis of differentiable functions  $f: \mathbb{C} \rightarrow \mathbb{C}$   
(instead of  $f: \mathbb{R} \rightarrow \mathbb{R}$ )

$\mathbb{R} \subseteq \mathbb{C} \Rightarrow$  helpful for real problems like  $\int_{-\infty}^{\infty} \frac{x \cdot \sin(x)}{1+x^2} dx = \frac{\pi}{e}$

We need:

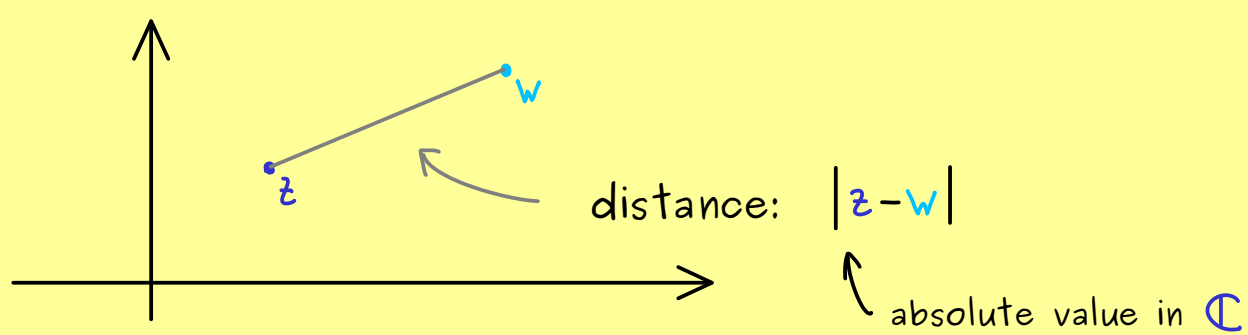
- sets
- complex numbers
- basic knowledge of continuous and differentiable functions
- basic knowledge of power series

Start Learning Mathematics

Real Analysis (some videos)

Some definitions:

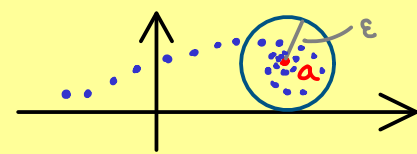
$\mathbb{C}$  is a set with a distance (metric space)



A sequence  $(z_n)_{n \in \mathbb{N}} \subseteq \mathbb{C}$  is convergent to  $a \in \mathbb{C}$

$\Leftrightarrow (|z_n - a|)_{n \in \mathbb{N}} \subseteq \mathbb{R}$  is convergent to 0

$\Leftrightarrow \forall \varepsilon > 0 \exists N \in \mathbb{N} \forall n \geq N : |z_n - a| < \varepsilon$



$\varepsilon$ -ball:  $\mathcal{B}_\varepsilon(a) := \{w \in \mathbb{C} \mid |w - a| < \varepsilon\}$

A function  $f: \mathbb{C} \rightarrow \mathbb{C}$  is continuous at  $z_0 \in \mathbb{C}$  if for all sequences  $(z_n)_{n \in \mathbb{N}} \subseteq \mathbb{C}$ :

$z_n \xrightarrow{n \rightarrow \infty} z_0$  implies  $f(z_n) \xrightarrow{n \rightarrow \infty} f(z_0)$ .

$\uparrow$  means:  $(z_n)_{n \in \mathbb{N}}$  is convergent to  $z_0$