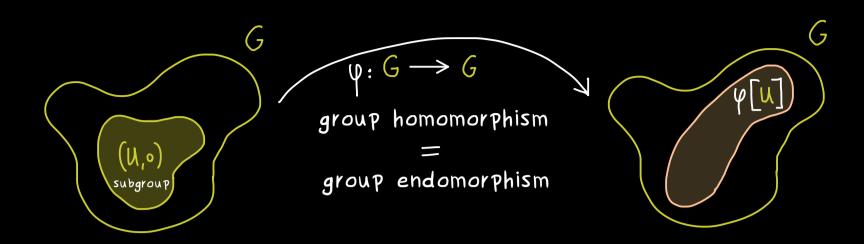


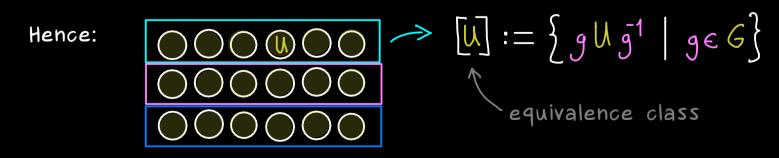
Algebra - Part 13



Important case: inner automorphisms: $\psi: G \longrightarrow G$ group homomorphism that endomorphism can be written as $\psi(x) = g \times g^{-1}$ is represented by an inner element bijective and homomorphism in both directions

We already know: $U \subseteq G$ subgroup $\Longrightarrow \varphi[U]$, $\varphi^1[U]$ subgroups

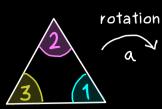
Remember: This defines an equivalence relation on the set of subgroups of G.



Trivial for abelian groups: $g U \bar{g}^{-1} = \{ u g \bar{g}^{-1} \mid u \in U \} = U$

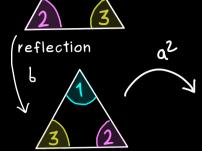
Example: Symmetric group S3

$$S_3 = \{e, a, b, a^2, ab, ba\}$$
reflection









$$U = \{e, b\} \xrightarrow{\text{conjugate subgroups}} a U \overline{a}^{1} = \{e, aba^{2}\} = \{e, ba\}$$

$$a^{2} U (a^{2})^{-1} = \{e, a^{2}ba\} = \{e, ab\}$$

$$ab U (ab)^{-1} = \{e, abb(ab)\} = \{e, ba\}$$

$$ba U (ba)^{1} = \{e, bab(ba)\} = \{e, ab\}$$

$$bU b^{-1} = eU e^{-1} = U$$