

Algebra - Part 2



Example: Set of functions $\mathcal{F}(\mathbb{R}) = \{ f \mid f: \mathbb{R} \to \mathbb{R} \text{ function} \}$ together with composition $\circ: \mathcal{F}(\mathbb{R}) \times \mathcal{F}(\mathbb{R}) \longrightarrow \mathcal{F}(\mathbb{R}):$ Take $f_1, f_2, f_3 \in \mathcal{F}(\mathbb{R})$ and define $g = f_1 \circ (f_2 \circ f_3) : \mathbb{R} \to \mathbb{R}$ $h = (f_1 \circ f_2) \circ f_3 : \mathbb{R} \to \mathbb{R}$ $g(x) = f_1 \circ (f_2 \circ f_3)(x) = f_1((f_2 \circ f_3)(x)) = f_1(f_2(f_3(x)))$ $h(x) = ((f_1 \circ f_2) \circ f_3)(x) = (f_1 \circ f_2)(f_3(x)) = f_1(f_2(f_3(x)))$ $\Longrightarrow (\mathcal{F}(\mathbb{R}), \circ)$ semigroup